

Lesson 2-6

Example 1 Find Probabilities of Simple Events

- a. Find the probability of rolling a number greater than 4 on a die.

There are 6 possible outcomes. Two of the outcomes are favorable.
That is, two of the six outcomes are greater than 4.

← 2 numbers greater than 4 →

Sample space: 1, 2, 3, 4, 5, 6

$\frac{2}{6}$

← 6 total possible outcomes →

$$\text{So, } P(\text{number greater than 4}) = \frac{2}{6} \text{ or } \frac{1}{3}$$

- b. An icosahedron has 20 sides numbered 1 through 20. The die is rolled once.
Find $P(\text{multiple of 5})$.

There are 4 multiples of 5 on the die and 20 total numbers.

$$\begin{aligned} P(\text{multiple of 5}) &= \frac{4}{20} && \leftarrow \text{ number of favorable outcomes} \\ & && \leftarrow \text{ number of possible outcomes} \\ &= \frac{1}{5} \text{ or } 0.20 && \text{Simplify.} \end{aligned}$$

The probability of rolling a multiple of 5 is $\frac{1}{5}$ or 20%.

- c. An icosahedron has 20 sides numbered 1 through 20. The die is rolled once.
Find $P(\text{not a multiple of 3})$.

There are 14 numbers that are not multiples of 3.

$$\begin{aligned} P(\text{not a multiple of 3}) &= \frac{14}{20} && \leftarrow \text{ number of favorable outcomes} \\ & && \leftarrow \text{ number of possible outcomes} \\ &= 0.70 && \text{Divide.} \end{aligned}$$

The probability of rolling a number that is not a multiple of 3 is $\frac{7}{10}$ or 70%.

- d. A card is selected at random from a standard deck of cards. Find $P(\text{king or jack})$

There are 4 ways to select a king and 4 ways to select a jack. So there are $4 + 4$ or 8 ways to select a king or a jack.

$$\begin{aligned} P(\text{king or jack}) &= \frac{8}{52} && \leftarrow \text{ number of favorable outcomes} \\ & && \leftarrow \text{ number of possible outcomes} \\ &\approx 0.15 && \text{Divide.} \end{aligned}$$

The probability of selecting a king or a jack is $\frac{2}{13}$ or about 15%.

Example 2 Odds of an Event

A bag contains 4 blue marbles, 6 red marbles, and 8 yellow marbles. One marble is chosen at random. Find the odds of choosing a blue marble.

There are 18 possible outcomes, 4 are successes and 14 are failures.

Sample space: 4 blue, 6 red, 8, yellow

4 marbles are blue	→	$\frac{4}{18}$
14 marbles are not blue	→	$\frac{14}{18}$

So, the odds of selecting a blue marble is $\frac{2}{7}$ or 2:7.

Example 3 Odds Against an Event

Find the odds against rolling a 5.

There is one 5 on a die and 6 – 1 or 5 numbers that are not five.

odds against a 5 = $\frac{5}{1}$ ← number of ways to not roll a 5
 ← number of ways to roll a 5

The odds against rolling a 5 on one die is 5:1.

Example 4 Probability and Odds

The probability for a baseball player to get a hit is 70%. What are the odds that he will get a hit at his next at bat?

The probability that he will get a hit is 70%, so the probability that he will not get a hit is 30%.

odds of getting a hit = 70:30 or 7:3

The odds that he will get a hit at his next at bat is 7:3.