

Exponential Functions (Pages 489–493)

Exponential Function

An **exponential function** is a function that can be described by an equation of the form $y = a^x$, where $a > 0$ and $a \neq 1$.

You can use ordered pairs to graph exponential functions. When you have graphed enough ordered pairs, connect the points to form a smooth curve. The graph of an exponential function changes little for small x -values, but as the values of x increase, the y -values increase quickly. The y -intercept of an exponential function is the y -coordinate of the point at which the graph crosses the y -axis. Exponential functions of the form $y = a^x$ have a y -intercept of 1. If a constant c is added to the function, it shifts the graph up or down c units.

EXAMPLES

Graph each exponential function. Then state the y -intercept.

A $y = 2^x + 1$

Make a table of values and then graph the function.

x	$2^x + 1$	y
-3	$2^{-3} + 1$	0.25
-2	$2^{-2} + 1$	0.5
-1	$2^{-1} + 1$	1
0	$2^0 + 1$	2
1	$2^1 + 1$	4
2	$2^2 + 1$	8



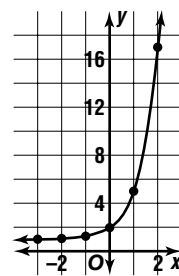
To find the y -intercept, let $x = 0$ and solve for y .

$$y = 2^0 + 1$$

In this case, the y -intercept is 2.

B $y = 4^x + 1$

x	$4^x + 1$	y
-3	$4^{-3} + 1$	≈ 1.02
-2	$4^{-2} + 1$	≈ 1.06
-1	$4^{-1} + 1$	1.25
0	$4^0 + 1$	2
1	$4^1 + 1$	5
2	$4^2 + 1$	17



The y -intercept is 2.

PRACTICE

Graph each exponential function. Then state the y -intercept.

1. $y = 2^x + 3$

2. $y = 2^x - 3$

3. $y = 2^x - 3$

4. $y = 3^x + 1$

5. $y = 4^x - 2$

6. $y = 0.5^x$

7. **Finance** Paola opened a savings account with a deposit of \$1000. The account pays an annual interest rate of 4%. How much money will be in Paola's account in 5 years?



8. **Standardized Test Practice** A bank account with an initial deposit of \$500 has a 5% annual interest rate. What is the balance in the account after 3 years?

A \$578.81

B \$575.00

C \$579.64

D \$545.00

Answers: 1–6. See Answer Key for graphs. 1. 4 2. $\frac{8}{1}$ 3. -2 4. 2 5. -1 6. 1 7. \$1216.65 8. A