

The Problem

José and Mike are members of a school video club. They were discussing sharing homemade videotapes. When José asked to borrow Mike’s videos, Mike replied: “Each video completely fills one videotape. I have just one videotape at home. However, I used to have lots of tapes. I gave $\frac{1}{2}$ of my videotapes plus $\frac{1}{2}$ a tape to JoAnne. I gave $\frac{1}{2}$ of my remaining videotapes and $\frac{1}{2}$ a tape to Maritza. Lastly, I gave $\frac{1}{2}$ of my remaining videotapes and $\frac{1}{2}$ a tape to Jeff.”

How many videotapes did Mike have originally? Why could JoAnne, Maritza, and Jeff watch all of the videotapes that Mike gave them?



Strategies and Hints

1. Be sure you understand the conditions of the problem. Discuss with others how Mike can share $\frac{1}{2}$ a videotape.
2. Try to solve the problem using smaller numbers of videotapes. For instance, you might try 7 or 8 tapes.
3. Make a chart using different numbers of videotapes.

Extension

If the video club used the procedure Mike followed and gave videotapes to 12 students, how many tapes did they have in their library?