

Lesson 9-6

Example 1 Use the Distance Formula

Find the distance between $M(1, 5)$ and $N(-3, 2)$. Round to the nearest tenth, if necessary.

Use the Distance Formula.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$MN = \sqrt{(-3 - 1)^2 + (2 - 5)^2}$$

$$MN = \sqrt{(-4)^2 + (-3)^2}$$

$$MN = \sqrt{16 + 9}$$

$$MN = \sqrt{25}$$

$$MN = 5$$

The distance between points M and N is 5 units.

Distance Formula

$$(x_1, y_1) = (1, 5), (x_2, y_2) = (-3, 2)$$

Simplify.

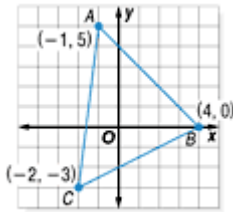
Evaluate $(-4)^2$ and $(-3)^2$.

Add 9 and 16.

Take the square root.

Example 2 Use the Distance Formula to Solve a Problem

GEOMETRY Find the perimeter of $\triangle ABC$ to the nearest tenth.



$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$AB = \sqrt{(4 - (-1))^2 + (0 - 5)^2}$$

$$AB = \sqrt{(5)^2 + (-5)^2}$$

$$AB = \sqrt{25 + 25}$$

$$AB = \sqrt{50}$$

Distance Formula

$$(x_1, y_1) = (-1, 5), (x_2, y_2) = (4, 0)$$

Simplify.

Evaluate 5^2 and $(-5)^2$.

Add 25 and 25.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$BC = \sqrt{(-2 - 4)^2 + (-3 - 0)^2}$$

$$BC = \sqrt{(-6)^2 + (-3)^2}$$

$$BC = \sqrt{36 + 9}$$

$$BC = \sqrt{45}$$

Distance Formula

$$(x_1, y_1) = (4, 0), (x_2, y_2) = (-2, -3)$$

Simplify.

Evaluate $(-6)^2$ and $(-3)^2$.

Add 36 and 9.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Distance Formula

$$CA = \sqrt{(-1 - (-2))^2 + (5 - (-3))^2}$$

$$(x_1, y_1) = (-2, -3), (x_2, y_2) = (-1, 5)$$

$$CA = \sqrt{1^2 + 8^2}$$

Simplify.

$$CA = \sqrt{1 + 64}$$

Evaluate 1^2 and 8^2 .

$$CA = \sqrt{65}$$

Add 1 and 64.

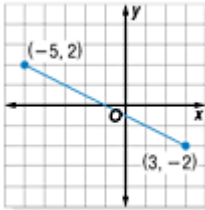
Then add the lengths of the sides to find the perimeter.

$$\begin{aligned}\sqrt{50} + \sqrt{45} + \sqrt{65} &\approx 7.071 + 6.708 + 8.062 \\ &\approx 21.841\end{aligned}$$

The perimeter is about 21.8 units.

Example 3 Use the Midpoint Formula

Find the coordinates of the midpoint of \overline{MN} .



$$\text{midpoint} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Midpoint Formula

$$= \left(\frac{-5 + 3}{2}, \frac{2 + (-2)}{2} \right)$$

Substitution

$$= (-1, 0)$$

Simplify.

The coordinates of the midpoint of \overline{MN} are $(-1, 0)$.